

General Form:

$${}^wA_t = {}^wA_0 \cdot {}^0A_A \cdot {}^A A_P \cdot {}^P A_t$$

B-Axis, single rotational offset in the Y direction, A axis and then the position vector

$${}^wA_0 = \begin{bmatrix} Cb & 0 & -Sb & 0 \\ 0 & 1 & 0 & 0 \\ Sb & 0 & Cb & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad {}^0A_A = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & Dy \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^A A_P = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & Ca & Sa & 0 \\ 0 & -Sa & Ca & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad {}^P A_t = \begin{bmatrix} 1 & 0 & 0 & Px \\ 0 & 1 & 0 & Py - Dy \\ 0 & 0 & 1 & Pz \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Gives:

$${}^wA_t = \begin{bmatrix} Cb & SaSb & -CaSb & CbPx - SaSb(Dy - Py) - CaSbPz \\ 0 & Ca & Sa & Dy - Ca(Dy - Py) + SaPz \\ Sb & -CbSa & CaCb & BcPx + CbSa(Dy - Py) + CaCbPz \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Looking at column 3 where:

$$K = \begin{bmatrix} K_x & -CaSb \\ K_y & Sa \\ K_z & CaCb \\ 0 & 0 \end{bmatrix}$$

Therefore

$$\theta_A = \sin^{-1} K_y$$

$$\theta_B = -\tan^{-1} \frac{K_x}{K_z}$$

Looking at the last column as the tool position vector:

$$Q = \begin{bmatrix} CbPx - SaSb(Dy - Py) - CaSbPz \\ Dy - Ca(Dy - Py) + SaPz \\ BcPx + CbSa(Dy - Py) + CaCbPz \\ 1 \end{bmatrix}$$

So I think I'm good up to here..... I have about 50% confidence in the next step:

$$Q = \begin{bmatrix} Q_x & Cb & SaSb & -CaSb & -SaSbDy & P_x \\ Q_y & 0 & Ca & Sa & (Ca - 1)Dy & P_y \\ Q_z & Sb & -CbSa & CaCb & CbSaDy & P_z \\ 1 & 0 & 0 & 0 & 1 & 1 \end{bmatrix}$$

Which I think should give an inverse matrix of:

$$\begin{bmatrix} P_x & Cb & 0 & Sb & 0 \\ P_y & SaSb & Ca & -CbSa & -DyCb^2Sa^2 - DySa^2Sb^2 + CaDy(Ca - 1) \\ P_z & -CaSb & Sa & CaCb & CaDySaCb^2 + CaDySaSb^2 + SaDy(Ca - 1) \\ 1 & 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} Q_x \\ Q_y \\ Q_z \\ 1 \end{bmatrix}$$